Efficient Location Based Services for Groups of Mobile Users





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Observation

 Mobile users send location updates to LBS server (back-end system; BES)

• The BES **pushes content** (possibly, personalized) to a mobile user **if** she enters/crosses a **region**





Observation

• As the **number** of mobile users increases, and

 As the users continuously change their position then

• The **communication overhead** for location reporting *and* location-based content delivery becomes quite significant

- Mobile users are not only close to each other but also likely to move together for a certain time horizon, thus, forming a moving group.
- A group has a unique **group leader** (GL).
- GL ... is the **representative** of the group, i.e.,
 - sends location updates to BES
 - **receives** possible location-dependent content and **disseminates** it to its members







Problem

- **How** to *evaluate* that a formed group *Q* at time *t*, will remain the **same** group at time *t*+*k*, *k*>1
- ...'same' group means:
 - **coherence**: group consists of the same mobile users as **initially** identified, and
 - **compactness**: all group members are **within** the communication range of the GL
 - during a *finite time horizon*



Group *Q* is defined as: $Q = \langle l, V_l \rangle$

 $\mathbf{c}_{Q} = \frac{1}{|Q|} \sum_{u \in O} \mathbf{p}_{u}$

 $l = \arg\min_{u \in Q} \left\| \mathbf{p}_u - \mathbf{c}_Q \right\| \quad \text{i.e., the GL of } Q$

i.e., the center point of Q

 $V_l = \left\{ u \mid \left\| \mathbf{p}_u - \mathbf{p}_l \right\| \le R \right\}$ i.e., the group members

Some Definitions

Group validity at (discrete) time *t*:

$$x_{t} = \left(\frac{1}{|\mathcal{Q}|} \sum_{u \in \mathcal{Q}} \left\|\mathbf{p}_{u}^{t} - \mathbf{c}_{\mathcal{Q}}^{t}\right\|\right) \cdot \boldsymbol{I}_{[\exists u \in V_{l}^{t}: \|\mathbf{p}_{u}^{t} - \mathbf{p}_{l}^{t}\| > R]} \left(V_{l}^{t}\right)$$

i.e., the average distance between members, *within the range of GL*, and group centroid

- Consider a *clustering algorithm*, which is invoked periodically **every** *N* time instances and produces a set of groups *Q* = {*Q*₁, *Q*₂, ..., *Q*_{|*Q*|}};
- Let $Q \in \mathbf{Q}$ be formed at t_0 . Q is **valid** at $t > t_0$ if $x_t \le \theta$
- The lower the x_t is, the more compact Q is at t

Group Validation System (GVS)
[1] monitors the behavior of Q in [t_o, k], i.e., checks whether Q maintains its *initial* structure.
[2] considers Q as a *persistent* group in (k, t_o + N]

At time t in $[t_0, k]$

(1) **each** member reports its location to BES; $f_t(|Q|)$ (2) GVS **evaluates** the group validity x_t ; $g_t(|Q|)$

(3) Total **cost**
$$c_t$$
 up to t is $c_t = \sum_{l=t_0}^t (f_l (|Q|) + g_l (|Q|))$

If GVS validates Q at k then for t in $(k, t_0 + N]$

(1) BES communicates only with GL;
 (2) only the GL reports its location to BES;
 (3) (possible) content is delivered to the members through the GL.



The problem is to find (an optimal) time k^* , $1 < k \le N$:

 $\inf_{1 < k \le N} E[X_k + c_k] = \inf_{1 < k \le N} E[X_k + kc]$

Optimal Stopping Theory

- Choose the **best** time instance to take a decision of performing a certain action.
- **Observe** the current state of a system and decide whether to:
 - continue the process or
 - > **stop** the process, and incur a certain **cost**.
- ...the *odds* algorithm, the *secretary* problem, the *parking* problem, the *asset-selling* problem, etc.

Application to Group Validity Process

- Adoption of Optimal Stopping Theory for evaluating an criterion for k^{*}.
- The more **validity** values the GVS *observes*, the more *certain* is on concluding on a 'group persistence'
- The GVS observes X_t at each t. The decision is:
 stop observing X_t and classify Q as persistent
 continue observing X_{t+1} with additional cost C
- 'Finite' Horizon GVS (FVS), i.e., $1 < k \le N$
- 'Infinite'-like Horizon GVS (IVS), i.e., 1 < k

'Finite' Horizon GVS (FVS)

- FVS should *validate Q* **up to** *N*.
- The criterion is the sequence (*a*₁, *a*₂, ..., *a*_N) such that FVS stops at *t* iff *x*_t < *a*_t

The {

$$a_t = a_{t+1} (P_X (X \le x) - P_X (X \le a_{t+1})) + \int_0^{a_{t+1}} x dP_X (x) + c$$
 h the
'princ $a_N = E[X] + c$ tion.

(FVS)





Performance Evaluation

Metric ε :communication overhead during N (total number of messages) w.r.t. a continuous monitoring system.

- For a *continuous* monitoring system: |Q|N
- For FVS is: $|Q|k^* + (N k^*)$
- For IVS is: $|Q|k^* + (Nm k^*)$; m^{-1} = re-validation rate
- For IMS (immediate validation system) is: N

IMS: **periodically** performs re-clustering with freq. 1/N



Performance Evaluation

Required communication load: $I_t = 1$, **if** Q is *valid* at t; $I_t \in (1, |Q|]$, **otherwise**;

i.e., the case in which some members are *not* within the communication range of the GL.

Metric *y* :efficiency is defined as:

$$\gamma = \frac{|Q|k^* + (N - k^*)}{|Q|k^* + \sum_{t=k^*}^N I_t} \qquad \gamma_{\max} \Leftrightarrow (N - k^*) = \sum_{t=k^*}^N I_t$$

Low γ indicates that the GVS **improperly** validated Q

The efficiency



Conclusions

There is **a trade-off** between:

- *validating* a group rapidly, thus, achieving low communication load (low ε) and
- *delaying* the validation decision for being certain on concluding on group persistence (high γ)

