## Crystal Maze

## coded in minizinc



Put a different number in each circle (1 to 8) such that adjacent circles cannot take consecutive numbers


Put a different number in each circle (0 to 7) such that adjacent circles cannot take consecutive numbers


Put a different number in each circle (0 to 7) such that adjacent circles cannot take consecutive numbers



> We are in the IDE







19 constraint abs(v1-v7) > 1;

20 constraint abs(v2-v3) > 1;
21 constraint abs(v2-v6) > 1;
22 constraint abs(v2-v7) > 1;
23 constraint abs(v3-v4) > 1;
19 constraint abs $(v 1-v 7)>1$,

24 constraint abs(v3-v7) > 1;
25 constraint abs(v4-v5) > 1;
26 constraint abs(v4-v6) > 1;
27 constraint abs(v4-v7) > 1;
28 constraint abs(v5-v6) > 1;
29 constraint abs(v5-v7) > 1;
30 constraint abs(v6-v7) > 1;

Configuration crystalMaze.mzn X

```
File Edit MiniZinc View Help
New model Open Save Copy
```


Configuration crystalMaze.mzn X
24 constraint abs(v3-v7) > 1;
25 constraint abs(v4-v5) > 1;
2 6 constraint abs(v4-v6) >1 All vertices take different values
27 constraint abs(v4-v7) > 1;
28constraint abs(v5-v6) > 1;
29 constraint abs(v5-v7) > 1;
30 constraint abs(v6-v7) > 1;
32include "alldifferent.mzn";
33constraint alldifferent([v0,v1,v2,v3,v4,v5,v6,v7]);
35solve satisfy;
36







## Can use command line

## Cin- Command Prompt

Y: \public_html \cpM\choco3\cpM\crystalMaze>minizinc crystalMaze.mzn
$v \square=1$
$v 1=5 ;$
v2
v3
v4
v5
v6
$=$
$=$
$=$
$=$
v7 = 0;

Y: \public_html \cpM\choco3\cpM\crystalMaze>_

## Can get all solutions

| ax Command Prompt | - | - | 口回 a |
| :---: | :---: | :---: | :---: |
| ```Y:\public_html\cpM\choco3\cpM\crystalMaze>minizinc crystalMaze.mzn -a v0 = 1; \vee1 = 5; \vee2 = 3; v4 = 2; \vee4 = 4; v6 = 7 v7 = 0;``` |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
| Y: \public_html \cpM\choco3\cpM\crystalMaze>_ |  |  |  |

## Can get statistics

Y: \public_html \cpM\choco3\cpM\crystalMaze>minizinc crystalMaze.mzn -s

| $0=$ |
| :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

74 choice points explored.
Y: \public_html \cpM\choco3\cpM\crystalMaze>

Let's make a more general model



```
Zñ crystalMaze1.mzn - Untitled Project
                                |-䓢
#File Edit MiniZinc View Help 
    1%
    2% Crystal Maze, second attempt, more general
    3%
    5 include "alldifferent.mzn";
    int: n; % number of vertices
    int: m; % number of edges
    array[1..m,1..2] of int: edge; % adjacency
    These are variables
    array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
    13 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
    constraint alldifferent(v);
    solve satisfy;
    output ["v = \(v)"];
    19
    n = 8;
    n = 8;
    m = 17;
    m = 17;
    edge \(=[\mid 0,1\)
        |0,5
        |0,6|
        |1,2
        |1,6
        |1,7
        |2,3
        2,6
        |2,7
        |3,4
        |3,7
        |4,5
        |4,6
        |4,7
        |5,6
        |5,7
        |6,7|]
    This is the data file, dzn extension

```

Zñ crystalMaze1.mzn — Untitled Project
|\square
File Edit MiniZinc View Help
Configuration crystalMaze1.mzn 区
1%
2% Crystal Maze, second attempt, more general
%
5 include "alldifferent.mzn";
I like to place this here
int: n; % number of vertices
int: m; % number of edges
array[1..m,1..2] of int: edge; % adjacency
array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
3 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
constraint alldifferent(v);
solve satisfy;
output ["v = \(v)"];
19







```
File Edit MiniZinc View Help
Configuration
crystalMaze1.mzn X
cm8.dzn X
1%
2% Crystal Maze, second attempt Hit run and it now allows me to select dzn file
5 include "alldifferent.mzn";
7int: n; % number of
8int: m; % number of
9array[1..m,1..2] of
10
11 array[0..n-1] of var
12
13 constraint forall(e
14 constraint alldiffer
|\textrm{Zn}\mathrm{ Model Parameters }
16 solve satisfy;
17
18 output ["v = \(v)"];
19
```

| File Edit MiniZinc View Help |
| :--- |
| $\square$ |

```
    1%
```

    1%
    2% Crystal Maze, second attempt, more general
    2% Crystal Maze, second attempt, more general
    3%
    3%
    include "alldifferent.mzn";
    include "alldifferent.mzn";
    int: n; % number of vertices
    int: n; % number of vertices
    sint: m; % number of edges
    sint: m; % number of edges
    array[1..m,1..2] of int: edge; % adjacency
    array[1..m,1..2] of int: edge; % adjacency
    10
    10
    array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
    array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
    constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
    constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
    constraint alldifferent(v);
    constraint alldifferent(v);
    1 5
    1 5
    solve satisfy;
    solve satisfy;
    1 7
    1 7
    output ["v = \(v)"];
    output ["v = \(v)"];
    Output
    Compiling crystalMaze1.mzn, with additional data cm8.dzn
Running crystalMaze1.mzn
$v=[1,5,3,6,2,4,7,0]$
Finished in 29 msec

> A solution for cm8.dzn

Y: \public_html $\backslash c \mathrm{c}_{\text {M }}$ \choco3\cpM\crystalMaze>minizinc crystalMaze1.mzn cm8.dzn $v=[1,5,3,6,2,4,7,0]$

Y: \public_html \cpM\choco3\cpM\crystalMaze>_

## Also on command line (all solutions)

cor. Command Prompt
Y: \public_html \cpM\choco3\cpM\crystalMaze>minizinc crystalMaze1.mzn cm8.dzn -a
$v=[1,5,3,6,2,4,7,0]$
v--------
2, 6, 3, 5, 7, 0]
$\mathrm{v}=[6,2,4,1,5,3,0,7]$
$\mathrm{v}=[6,3,5,1,4,2,0,7]$
-----------
===========
Y: \public_html \cpM\choco3\cpM\crystalMaze>

## Compare two models ... cool

```
Command Prompt
Y:\public_html\cpM\choco3\cpM\crystalMaze>minizinc crystalMaze.mzn -s
v0 = 1;
v1 = 5
v
v6
7 = 0;
% 74 choice points explored.
Y: \public_html\cpM\choco3\cpM\crystalMaze>minizinc crystalMaze1.mzn cm8.dzn -s
v = [1, 5, 3, 6, 2, 4, 7, 0]
% }74\mathrm{ choice points explored.
Y:\public_html\cpM\choco3\cpM\crystalMaze>_
```



| Configuration | crystalMaze 1．mzn ${ }^{\text {® }}$ | cm8．dzn 区 | cm11．dzn 区 |
| :---: | :---: | :---: | :---: |



## Configuration

 crystalMaze1.mzn $X$ cm8.dzn cm11.dzn Х1\%
\% Crystal Maze, second attempt, more general
$3 \%$
include "alldifferent.mzn";

7int: $n$; \% number of vertices
8 int: m; \% number of edges
array[1..m,1..2] of int: edge; \% adjacency

$$
0
$$

$$
\text { array }[0 . . n-1] \text { of } \operatorname{var} 0 \ldots n-1: v ; \% \text { vertices } v[0] \text { to } v[n-1]
$$

$$
2
$$

constraint forall(e in 1..m)(abs(v[edge[e,1]]-v[edge[e,2]])>1);
constraint alldifferent(v);

```
solve satisfy;
```

    output ["v = \\(v)"];
    19
    $v=[1,6,3,6,2,4,1,0]$
Finished in 29 msec
Compiling crystalMaze1.mzn, with additional data cm11.dzn
Running crystalMaze1.mzn
$v=[1,8,6,10,4,9,5,7,3,0,2]$
Finished in 27msec

Y: \publichtml \cpM\choco3\cpM\crystalMaze>minizinc crystalMaze1.mzn cm11.dzn $v=[1,1 \overline{0}, 5,8,3,6,4,9,7,2,0]$

Y: \public_html \cpM\choco3\cpM\crystalMaze>_

## Ouch! (-a on cm11)

| $\mathrm{V}=[3,1$, | $10,7,5,9,2,6,8,4,01$ |
| :---: | :---: |
| $\mathrm{v}=[3,1$, | 10, 7, 5, 9, 2, 8, 6, 4, 0] |
| $\mathrm{v}=[3,1$, | 10, 7, 5, 8, 2, 9, 6, 4, 0] |
| $\mathrm{v}=[3,8$, | $10,7,5,2,9,6,1,4,0]$ |
| $\mathrm{v}=[3,8$, | 10, 7, 5, 2, 9, 1, 6, 4, 0] |
| $\mathrm{v}=[3,8$ | 10, 7, 5, 2, 6, 9, 1, 4, 0] |
| $\mathrm{v}=\mathrm{L5}$, 9 | 2, 6, 3, 8, 10, 1, 7, 4, 0] |
| = [5, 8, | 2, 6, 3, 9, 7, 1, 10, 4, 0] |
| [3, 8, | 6, 10, 5, 2, 7, 9, 1, 4, 0] |

solution received from solver: 2 :
$\vee$ ㅊ array1d(0..10, [3, 1, 6, 10, 5, 8, 2, 7, 9, 4, 0]);
Error: syntax error, unexpected =, expecting ':'
MiniZinc: internal error: not sm.get(): solnsZout_base: could not parse solution flatzinc: I/O error: error writing to output file: Invalid argument minizinc: evaluation killed by signal 1

Y: \public_html\cpM\choco3\cpM\crystalMaze〉

So, what IS a constraint program?

## Possible answers

It's a program that generates variables and constraints to represent a problem

It's a program that creates a model of a problem and then uses search and heuristics to solve the problem

It's a program that compiles some problem into a representation as CSP

