# Crystal Maze

# coded in minizinc



Put a different number in each circle (1 to 8) such that adjacent circles cannot take consecutive numbers



Put a different number in each circle (0 to 7) such that adjacent circles cannot take consecutive numbers

### The numbers are the identification of a circle



Put a different number in each circle (0 to 7) such that adjacent circles cannot take consecutive numbers



1<sup>st</sup> stab ...



#### We are in the IDE











Zn crystalMaze.mzn — Untitled Project	
<u>F</u> ile Edit MiniZinc View Help	
New model Open Save Copy Out Paste Undo Redo Shiftleft Shiftright Run Stop	
	brion project explorer
<pre>19 constraint abs(v1-v7) &gt; 1;</pre>	•
<pre>20 constraint abs(v2-v3) &gt; 1;</pre>	
<pre>21 constraint abs(v2-v6) &gt; 1;</pre>	
<pre>22 constraint abs(v2-v7) &gt; 1;</pre>	
<pre>23 constraint abs(v3-v4) &gt; 1; Couldn't get them on 1</pre>	screen
<pre>24 constraint abs(v3-v7) &gt; 1;</pre>	
<pre>25 constraint abs(v4-v5) &gt; 1;</pre>	
<pre>26 constraint abs(v4-v6) &gt; 1;</pre>	=
<pre>27 constraint abs(v4-v7) &gt; 1;</pre>	
<pre>28 constraint abs(v5-v6) &gt; 1;</pre>	
<pre>29 constraint abs(v5-v7) &gt; 1;</pre>	
<pre>30 constraint abs(v6-v7) &gt; 1;</pre>	
	▼ ■ X

Zn crystalMaze.mzn — Untitled Project	
<u>F</u> ile Edit MiniZinc View Help	
Image: New model       Open       Save       Copy       Cut       Paste       Undo       Redo       Shift left       Shift right       Run       Stop	Show project explorer
Configuration crystalMaze.mzn 🗵	
<pre>24 constraint abs(v3-v7) &gt; 1;</pre>	^
<pre>25 constraint abs(v4-v5) &gt; 1;</pre>	
26 constraint abs(v4-v6) > 1 All vertices take different	nt values
<pre>27 constraint abs(v4-v7) &gt; 1;</pre>	
<pre>28 constraint abs(v5-v6) &gt; 1;</pre>	
<pre>29 constraint abs(v5-v7) &gt; 1;</pre>	
<pre>30 constraint abs(v6-v7) &gt; 1;</pre>	
31	
<pre>32 include "alldifferent.mzn";</pre>	
<pre>33 constraint alldifferent([v0,v1,v2,v3,v4,v5,v</pre>	/6,v7]);
34	
35 solve satisfy;	
36	
	~
Output	5 ×
	in.



Zn crystalMaze.mzn — Untitled Project	
<u>File</u> Edit MiniZinc View Help	
Image: New model       Open       Save       Copy       Cut       Paste       Undo       Redo       Shift left       Shift right       Run       Stop	Show project explorer
Configuration crystalMaze.mzn 🗵	
<pre>24 constraint abs(v3-v7) &gt; 1;</pre>	A
<pre>25 constraint abs(v4-v5) &gt; 1;</pre>	
<pre>26 constraint abs(v4-v6) &gt; 1;</pre>	
<pre>27 constraint abs(v4-v7) &gt; 1;</pre>	
<pre>28 constraint abs(v5-v6) &gt; 1;</pre>	
<pre>29 constraint abs(v5-v7) &gt; 1;</pre>	
<pre>30 constraint abs(v6-v7) &gt; 1;</pre>	
31	
<pre>32 include "alldifferent.mzn";</pre>	
<pre>33 constraint alldifferent([v0,v1,v2,v3,v4,v5,v</pre>	/6,v7]);
34	-
35 solve satisfy; Get me a solution	n
- 30	-
	-
Output	₽ ×



Zn crystalMaze.mzr	n — Untitled Pro	ject		-	-			
<u>F</u> ile Edit MiniZ	Zinc View H	elp						
New model Open	Save Copy	Cut Paste	Undo Redo	Shift left	Shift right	⊳ Run	Stop	Show project explorer
Configuration C	rystalMaze.mzn [	3						
3 % 4 5 var 07: 6 var 07: 7 var 07: 8 var 07: 9 var 07: 10 var 07: 11 var 07: 12 var 07: 13 14 constraint	<pre>v0; v1; v2; v3; v4; v5; v6; v7; t abs(v0-v1 t abs(v0-v5</pre>	.) > 1; ;; > 1;						
Output								5 ×
Compiling cr Running crys v0 = 1; v1 = 5; v2 = 3; v3 = 6; v4 = 2; v5 = 4; v6 = 7; v7 = 0; 	rystalMaze. stalMaze.mz 29msec	mzn n			Here	e's a	solution (not un	ique).
								29msec





#### Can use command line



Can get all solutions

Command Prompt			
Y:\public_html\cpM\choco3\cpM v0 = 1; v1 = 5; v2 = 3; v3 = 6; v4 = 2; v5 = 4; v6 = 7; v7 = 0;	1∖crystalMaze>mini	zinc crystalMaze.mzn	-a
<pre>&gt;0 = 1;; &gt;14;; &gt;15;; &gt;14;; &gt;15;; &gt;14;; &gt;15;; &gt;14;; &gt;15;</pre>			
<pre>&gt;010000000000000000000000000000000000</pre>			
========== Y:\public_html\cpM\choco3\cpM	1∖crystalMaze>_		
· · · · · · · · · · · · · · · · · · ·			

## Can get statistics

Command Prompt	
Y:\public_html\cpM\choco3\cpM\crystalMaze>minizinc crystalMaze.mzn - v0 = 1; v1 = 5; v2 = 3; v3 = 6; v4 = 2; v5 = 4; v6 = 7; v7 = 0;	-5
% % 74 choice points explored. %	
Y:\public_html\cpM\choco3\cpM\crystalMaze>	
	E. I

Let's make a more general model



```
X
Zn crystalMaze1.mzn — Untitled Project
File Edit MiniZinc View Help
                          Paste Undo Redo Shift left Shift right
New model
       Open Save
                      Cut
                                                     Run
                                                         Stop
                                                                                       Show project explorer
                 Copy
           crystalMaze 1.mzn 🔀
 Configuration
  1%
  2% Crystal Maze, second attempt, more general
  3 %
   5 include "alldifferent.mzn";
   7 int: n; % number of vertices
  8 int: m; % number of edges
   g array[1..m,1..2] of int: edge; % adjacency
  10
  11 array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
  12
  13 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
  14 constraint alldifferent(v);
  15
 16 solve satisfy;
 17
 18 output ["v = (v)"];
  19
                                                                                                 8×
Output
Ready.
```

```
X
Zn crystalMaze1.mzn — Untitled Project
File Edit MiniZinc View Help
New model
       Open
            Save
                      Cut
                          Paste Undo
                                  Redo Shift left Shift right
                                                                                       Show project explorer
                 Copy
                                                    Run
                                                         Stop
           crystalMaze 1.mzn 🔀
 Configuration
  1%
  2% Crystal Maze, second attempt, more general
  3 %
  5 include "alldifferent.mzn";
  7 int: n; % number of vertices
  8 int: m; % number of edges
                                                                     These are variables
  garray[1..m,1..2] of int: edge; % adjacency
  11 array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
  12
  13 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
  14 constraint alldifferent(v);
  15
  16 solve satisfy;
 17
  18 output ["v = (v)"];
  19
                                                                                                 8×
Output
Ready.
```





```
X
Zn crystalMaze1.mzn — Untitled Project
File Edit MiniZinc View Help
New model
       Open
                      Cut
                          Paste Undo
                                   Redo Shift left Shift right
                                                                                        Show project explorer
            Save
                 Copy
                                                     Run
                                                         Stop
           crystalMaze 1.mzn 🔀
 Configuration
  1 %
  2% Crystal Maze, second attempt, more general
  3 %
                                                              I like to place this here
   5 include "alldifferent.mzn";
   7 int: n; % number of vertices
  8 int: m; % number of edges
   g array[1..m,1..2] of int: edge; % adjacency
  10
  11 array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
  12
  13 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
  14 constraint alldifferent(v);
  15
  16 solve satisfy;
  17
 18 output ["v = (v)"];
  19
                                                                                                 8×
Output
Ready.
```













Zn crystalMaze1.mzn — Untitled Project			
<u>F</u> ile Edit MiniZinc View Help			
New model Open Save Copy Cut Paste L	Jndo Redo Shift left Shift right Ru	> 🗌 n Stop	Show project explorer
Configuration crystalMaze1.mzn C cm8.dzn	<u>1</u>		
1% 2% Crystal Maze, second a 3%	ttempt: Hit run and it	now allows me to sele	ct dzn file
<pre>5 include "alldifferent.mz</pre>	n";		
<pre>6 7 int: n; % number of 8 int: m; % number of 9 array[1m,12] of 10 11 array[0n-1] of var 12 13 constraint forall(e 14 constraint alldiffere 15 16 solve satisfy; 17 18 output ["v = \(v)"]; 19</pre>	odel Parameters elect data file or input values =   ge =	<pre>     X     OK Cancel     &gt; 1); </pre>	
Output			5 ×
Ready.			16s 888msec

```
X
Zn crystalMaze1.mzn — Untitled Project
File Edit MiniZinc View Help
                                                                Redo Shift left Shift right
                                                                                                 Show project explorer
New model Open Save
                        Cut
                            Paste Undo
                   Cody
                                                           Run
                                                               Stop
 Configuration
            crystalMaze 1.mzn 🔀
                            cm8.dzn 🖂
  1 %
  2% Crystal Maze, second attempt, more general
  3 %
  5 include "alldifferent.mzn";
  7 int: n; % number of vertices
  8 int: m; % number of edges
  9 array[1..m,1..2] of int: edge; % adjacency
 11 array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
  12
 13 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
  14 constraint alldifferent(v);
  15
 16 solve satisfy;
  17
 18 output ["v = (v)"];
                                                                                                            ₽×
Output
 Compiling crystalMaze1.mzn, with additional data cm8.dzn
 Running crystalMaze1.mzn
 v = [1, 5, 3, 6, 2, 4, 7, 0]
                                                           A solution for cm8.dzn
 Finished in 29msec
                                                                                                        29msec
Ready.
```

Also on command line



### Also on command line (all solutions)



Compare two models ... cool

```
Command Prompt
                                                                           . .
  \public_html\cpM\choco3\cpM\crystalMaze>minizinc crystalMaze.mzn -s
= 1;
                                                                                           ٠
                                                                                           Ξ
   0;
   バンン
  74 choice points explored.
Y:\public_html\cpM\choco3\cpM\crystalMaze>minizinc crystalMaze1.mzn cm8.dzn -s
  = [1, 5, 3, 6, 2, 4, 7, 0]
/
//
  74 choice points explored.
Y:\public_html\cpM\choco3\cpM\crystalMaze>_
                           111
```



```
- O X
Zn crystalMaze1.mzn — Untitled Project
File Edit MiniZinc View
                      Help
                                       Redo Shift left Shift right
                                                                                                  Show project explorer
New model Open Save
                         Cut
                             Paste
                                  Undo
                   Cody
                                                           Run
                                                                Stop
 Configuration
            crystalMaze 1.mzn 🔀
                            cm8.dzn 🗵
                                       cm11.dzn 🖂
  1 %
  2% Crystal Maze, second attempt, more general
  3 %
  5 include "alldifferent.mzn";
  7 int: n; % number of vertices
  8 int: m; % number of edges
  garray[1..m,1..2] of int: edge; % adjacency
 11 array[0..n-1] of var 0..n-1: v; % vertices v[0] to v[n-1]
 12
 13 constraint forall(e in 1..m)(abs(v[edge[e,1]] - v[edge[e,2]]) > 1);
 14 constraint alldifferent(v);
  15
 16 solve satisfy;
 17
 18 output ["v = (v)"];
 19
                                                                                                             8×
Output
 v = [1, 5, 3, 6, 2, 4, 7, 0]
                                                                                                              ۰
 Finished in 29msec
 Compiling crystalMaze1.mzn, with additional data cm11.dzn
 Running crystalMaze1.mzn
                                                                                                              A solution for cm11.dzn
 v = [1, 8, 6, 10, 4, 9, 5, 7, 3, 0, 2]
 Finished in 27msec
                                                                                                         27msec
Ready.
```



### Ouch! (-a on cm11)



## So, what IS a constraint program?

### Possible answers

It's a program that generates variables and constraints to represent a problem

It's a program that creates a model of a problem and then uses search and heuristics to solve the problem

It's a program that compiles some problem into a representation as CSP