## Abarth Paint Shop

In the Abarth paint shop cars can be :

grey<br>red<br>white<br>yellow<br>blue ... or<br>black







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Configuration abarth595.dzn ® abarth595.mzn ®
satisfaction (maybe unsat!)
satisfaction (maybe unsat!)
9%
9%
10include "globals.mzn";
10include "globals.mzn";
2enum ALLCOLOURS = {grey,red,white,yellow,blue,black,BLANK};
2enum ALLCOLOURS = {grey,red,white,yellow,blue,black,BLANK};
3set of ALLCOLOURS: COLOURS = ALLCOLOURS diff {BLANK};
3set of ALLCOLOURS: COLOURS = ALLCOLOURS diff {BLANK};
14array[COLOURS] of int: maxRun = [3,4,4,3,2,3];
14array[COLOURS] of int: maxRun = [3,4,4,3,2,3];
15array[ALLCOLOURS,ALLCOLOURS] of 0..1: transition = [|1,1,1,0,1,1,1 % grey
15array[ALLCOLOURS,ALLCOLOURS] of 0..1: transition = [|1,1,1,0,1,1,1 % grey
16
16
1 7
1 7
18
18
19
19
20
20
21
21
| |,1,0,0,1,1,1}<ll
| |,1,0,0,1,1,1}<ll

```
When painting cars ...
```

- 3 grey cars can be painted one after the other
- 4 red can be painted one after the other
- 4 white can be painted one after the other
- 3 yellow one after the other
- 2 blue one after the other
- 3 black one after the other
Zñ abarth595.mzn — Untitled Project
Show project explorer
Configuration abarth595.dzn 』 abarth595.mzn ®
satisfaction (maybe unsat!)
9\%
10include "globals.mzn";
11
12 enum $\operatorname{ALLCOLOURS~}=$ \{grey, red, white, yellow, blue, black, BLANK $\} ;$

4 array[COLOURS] of int: maxRun $=[3,4,4,3,2,3]$;
15 array[ALLCOLOURS, ALLCOLOURS] O+ 0..1: transition $=[\mid 1,1,1,0,1,1,1$

$$
\begin{array}{ll}
\mid 0,1,0,0,1,1,1 & \text { \% red } \\
\mid 1,1,1,1,0,0,1 & \text { \% white } \\
\mid 0,0,1,1,0,0,1 & \text { \% yellow } \\
\mid 1,0,0,0,1,1,1 & \text { \% blue } \\
\mid 0,0,0,0,0,1,1 & \text { \% black } \\
|1,1,1,1,1,1,1|] ; & \text { \% BLANK }
\end{array}
$$

```
When changing colours ...
```

- After grey we can paint grey, red, white, blue, black or BLANK
- After red we can paint red, blue, black or BLANK
- After white we can paint white, grey, red, yellow or BLANK
- After yellow we can paint yellow, white or BLANK
- After blue we can paint blue, black or BLANK
- After black we can paint black or BLANK
- After BLANK we have clean paint guns and can paint any colour
Zn abarth595.mzn — Untitled Project
Configuration abarth595.dzn 』 abarth595.mzn 『
satisfaction (maybe unsat!)
$9 \%$
10include "globals.mzn";
11
12 enum ALLCOLOURS $=$ \{grey, red, white, yellow, blue, black, BLANK $\}$
13 set of ALLCOLOURS: COLOURS = ALLCOLOURS diff \{BLANK\};
1^annav[COIOURC] of int. mavRun - [2 1 1 2 2].

$$
\begin{aligned}
& \text { array[ALLCOLOURS,ALLCOLOURS] of 0..1: transition }=[\mid 1,1,1,0,1,1,1 \% \text { grey } \\
& \mid 0,1,0,0,1,1,1 \text { \% red } \\
& \mid 1,1,1,1,0,0,1 \quad \% \text { white } \\
& \mid 0,0,1,1,0,0,1 \text { \% yellow } \\
& \mid 1,0,0,0,1,1,1 \text { \% blue } \\
& \mid 0,0,0,0,0,1,1 \text { \% black } \\
& |1,1,1,1,1,1,1|] ; \% \text { BLANK }
\end{aligned}
$$

We have a demand for cars of these colours and an allowed time to paint them ...


```
Decision variables ...
```

Given a time line, at each time slot, what colour of car will we paint?

## Decision variables ...

```
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```



```
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    Show project explorer
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abarth595.mzn 『
22
23% input parameters
24array[COLOURS] of int: demand;
25int: timeLimit;
27% our decision variables ... what colour (maybe BLANK) in a time slot
28array[1..timeLimit] of var ALLCOLOURS: timeLine; % value is a colour
30% only valid transitions allowed!
31constraint forall(t in 1..timeLimit-1)(transition[timeLine[t],timeLine[t+1]] = 1);
32
33% meet demands exactly!
34constraint forall(colour in COLOURS)(exactly(demand[colour],timeLine,colour));

\section*{Decision variables ...}
```

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```


```

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```
timeLine[t] = colour <-> a car of that colour is painted at time t
```



When we change colours, transitions, they must be valid

## Colour transitions must be valid ...

```
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```




```
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23% input parameters
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```
```

Output

```
```

Output

```

\section*{Colour transitions must be valid ...}
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34constraint forall(colour in COLOURS)(exactly(demand[colcur],timeLine,colour));
These are colours!
Using constrained integer variable as array index!

```

Demand for each colour must be met, exactly !!!!

Meet demand exactly ...

\section*{Demand for each colour must be met, exactly !!!!}
```

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Show project explorer
Configuration abarth595.dzn \boxtimes abarth595.mzn ®
1%
2% abarth paint shop
3% available colours {grey,red,white,yellow,blue,black};
5% demand for each colour
demand = [4,2,3,5,2,4];
7% now muc! cHme we Trave co meet above demand
8timeLimit = 30; % minimum is 21
9%
10% NOTE: problem instance may be unsat (unsatisfiable)
11%

```
Output

\section*{Demand for each colour must be met, exactly !!!!}
```

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NOTE: no demand for BLANK © ;

```

enum ALLCOLOURS = {grey,red,white,yellow,blue,black,BLANK};
set of ALLCOLOURS: COLOURS = ALLCOLOURS diff {BLANK};
array[COLOURS1 of int: maxRun = 「3,4,4,3,2,31;

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```

\section*{The maximum run of each colour ...}
```

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New model Open Save Copy Cut Paste Undo Redo Shift left Shift right Run Stop
Show project explorer
Configuration abarth595.dzn « abarth595.mzn * «
constraint forall(t in 1..timeLimit-1)(transition[timeLine[t],timeLine[t+1]] = 1);
% meet demands exactly!
constraint forall(colour in COLOURS)(exactly(demand[colour],timeLine,colour));
% respect max run for each colour.
constraint forall(colour in COLOURS, t in 1..timeLimit - maxRun[colour])
(at_most(maxRun[colour],[timeLine[i] | i in t..t+maxRun[colour]],colour));
% can't start by doing nothing!
Output

```

\section*{The maximum run of each colour ...}


\section*{The maximum run of each colour ...}
```

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6% respect max run for each colour.
7constraint forall(colour in COLOURS, t in 1..timeLimit - maxRun[colour])
(at_must(maxkum[colvur],[tametine[1] | I Int (..t+maxrum[colour]],colour));
40% can't start by doing nothing!
41constraint timeLine[1] != BLANK;
42
For each colour, and for each colour the sliding time window ...

```

\section*{The maximum run of each colour ...}

```

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Configuration abarth595.dzn @ abarth595.mzn * «
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33% meet demands exactly!
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35
36% respect max run for each colour.
constraint foralf(comour In colouks, l In l..cimelaml( - maxkun[colour])
(at_most(maxRun[colour],[timeLine[i] | i in t..t+maxRun[colour]],colour))
39
%% can't start by doing nothing!
constraint timeLine[1] != BLANK;

## For that colour, and that time window starting at t ...

``` there must be at most maxRun[colour] of that colour!
```


## The maximum run of each colour ...

```
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    constraint foralf(comour In colouks, l In l..cimelaml( - maxkun[colour])
                (at_most(maxRun[colour],[timeLine[i] | i in t..t+maxRun[colour]],colour))
    39
    % can't start by doing nothing!
    constraint timeLine[1] != BLANK;
```

NOTE: on-the-fly array comprehension ©

[^0]Don't start the day by doing nothing!

## Dinnae hing aboot ...

```
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```



```
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Configuration abarth595.dzn « abarth595.mzn * «
    37constraint forall(colour in COLOURS, t in 1..timeLimit - maxRun[colour])
(at_most(maxRun[colour],[timeLine[i] | i in t..t+maxRun[colour]],colour));
    40% can't start by doing nothing!
    41 constraint timeLine[1] != BLANK;
    43% when you're done you're done!
    44constraint forall(t in 1..timeLimit-2)(timeLine[t] = BLANK /\ timeLine[t+1] = BLANK -> timeLine[t+2] = BLANK);
45
    46Solve satisfy;
```

Output

When you're done you're done ...

## When you're done you're done ...

```
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```

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Configuration abarth595.dzn @ abarth595.mzn*@
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                    (at_most(maxRun[colour],[timeLine[i] | i in t..t+maxRun[colour]],colour));
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    40% can't start by doing nothing!
    41 constraint timeLine[1] != BLANK;
    % when you're done you're done!
    constraint forall(t in 1..timeLimit-2)(timeLine[t] = BLANK /\ timeLine[t+1] = BLANK -> timeLine[t+2] = BLANK);
```

    46Solve satisfy;
    Output
black, BLANK, grey
[4, 2, 3, 5, 2, 4]
\% runtime:
runtime:
solvetime:
solutions:
solutions:
variables
propagators: $\quad 115$
propagations: 1023
nodes:
failures:
restarts:
\%\% peak depth:
$0.015(15.000 \mathrm{~ms})$
$0.000(0.000 \mathrm{~ms})$

P C: 14
PS C:\cpM\minizincCPM\paintshop>


## 2. Windows PowerShell

## $\%$ runtime:

solvetime:
solutions
variables:
propagators:
propagations:
nodes:
failures
failures:
restarts
\%\% peak depth:
$0.252(252.000 \mathrm{~ms})$
$0.239(239.000 \mathrm{~ms})$
1.

79
189

17934
1793
0
33
33
PS C:\cpM\minizincCPM\paintshop>

Can you think of a different model?

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| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ¢（i）www．minizinc．org／doc－lib／doc－globals－extensional．html | § | C | Q Se |  |  | $\pm$ | 自 | $\checkmark$ | $\downarrow$ | ก | \％\％ | 三 |
| Zñ MiniZinc | Software |  |  | Resources | Team | Challenge |  | Discussions |  |  |  |  |

## MiniZinc Documentation－Standard Library

Extensional constraints（table，regular etc．）
（（1）Index reveal all hide all

```
predicate regular(array [int] of var int: x
    int: Q,
    int: S,
    array [int,int] of int: d,
    int: q0,
    set of int: F)
```

The sequence of values in array $\mathbf{x}$（which must all be in the range $1 . . S$ ）is accepted by the DFA of $Q$ states with input 1 ．．$S$ and transition function $d$（which maps（1．．Q，1．．S）－＞ $0 . . Q$ ）and initial state $\mathrm{q}_{0}$（which must be in $1 . . Q$ ）and accepting states $F$（which all must be in $1 . . Q$ ）． We reserve state 0 to be an always failing state．

```
predicate regular_nfa(array [int] of var int: x,
    int: Q,
    int: S,
    array [int,int] of set of int: d,
    int: q0,
    set of int: F)
```

|  | gray | red | white | yelba | blue | black | BLANK |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| grey | 1 | 1 | 1 | 0 | 1 | 1 | 1 |
| red | 0 | 1 | 0 | 0 | 1 | 1 | 1 |
| white | 1 | 1 | 1 | 1 | 0 | 0 | 1 |
| yellow | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| blue | 1 | 0 | 0 | 0 | 1 | 1 | 1 |
| blat | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| BLANK | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| MaaRum | 3 | 4 | 4 | 3 | 2 | 3 | $*$ |



```
%
% Paint shop version Regular
%
include "globals.mzn";
enum ALLCOLOURS = {grey,red,white,yellow,blue,black,BLANK};
set of ALLCOLOURS: COLOURS = ALLCOLOURS diff {BLANK};
% input parameters
array[COLOURS] of int: demand;
int: timeLimit;
% our decision variables ... what colour (maybe BLANK) in a time slot
array[1..timeLimit] of var ALLCOLOURS: timeLine; % value is a colour
% meet demands exactly!
constraint forall(colour in COLOURS)(exactly(demand[colour],timeLine,colour));
%
% Now use a regular constraint ...
%
solve satisfy;
```


[^0]:    Dinnae hing aboot ...

